Chapter 1 Investigating data distributions: Assignment

Student name: _____

The table below gives the distribution of waiting times of 39 cars at a set of traffic lights 1 on a major road on a Sunday afternoon.

| Time spent waiting | Frequency | Percentage |
|--------------------|-----------|------------|
| (seconds) | | |
| 0-4 | 1 | 2.6 |
| 5–9 | 3 | 7.7 |
| 10–14 | 2 | 5.1 |
| 15–19 | 2 | 5.1 |
| 20–24 | 3 | 7.7 |
| 25–29 | 6 | 15.4 |
| 30–34 | | 20.5 |
| 35–39 | 9 | |
| 40–44 | 4 | 10.3 |
| 45–49 | 0 | 0 |
| 50–54 | 0 | 0 |
| 55–59 | 1 | 2.6 |
| Total | 39 | 100.1 |

- Complete the table by filling in the blank spaces. a
- Determine: b
 - i the number of cars that waited at the lights for less than 25 seconds
 - the percentage of cars that waited at the lights for 40 seconds or more ii
- Use the grid below to construct a frequency histogram to display the distribution of c waiting times. Label your axes appropriately.

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- i Use your histogram to help you describe the shape of the distribution of waiting times.
- We wish to calculate a measure of centre to enable us to estimate the typical ii waiting times of cars stopping at these traffic lights on a Sunday. Given the shape of the distribution of waiting times, which measure of centre is most appropriate to use and what is its approximate value?
- The following table gives the life expectancies in years for females from 28 countries 2 around the world.

| 62.3 | 78.7 | 76.0 | 71.5 | 58.6 | 80.8 | 71.3 | 47.5 | 81.4 | 80.7 | 54.1 | 82.0 | 82.8 | 50.5 |
|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 43.2 | 81.9 | 75.7 | 72.1 | 78.7 | 72.0 | 78.3 | 69.1 | 53.4 | 81.2 | 80.7 | 81.6 | 82.0 | 84.1 |

- Use your calculator to construct a histogram of the female life expectancies, with a a starting point of 40 and an interval width of 5. Use the histogram on your calculator to answer the following questions.
 - i What is the shape of the histogram?
 - ii How many countries have female life expectancies of less than 60 years?
 - How many countries have female life expectancies of less than 70 years? iii
 - How many countries have female life expectancies of 80 years or more? iv

- **b** Use your calculator to help you complete the following statements by calculating the appropriate statistics:
 - The mean life expectancy for females is _____ and the standard deviation of life i expectancies is .
 - 50% of these countries have female life expectancies less than or equal to ii
 - iii The range of female life expectancies was
 - iv 25% of these countries recorded female life expectancies less than .
 - 25% of these countries recorded female life expectancies greater than v
 - vi The interquartile range for female life expectancies is
 - vii To be an outlier a country would need to have a female life expectancy of less than or more than _____ .
- Of the 39 cars that stopped at a set of traffic lights, 15 continued along the road until they 3 reached the next set of traffic lights, two kilometres down the road. The five number summary for their travelling times is:

Q1 = 2.0 M = 2.6 Q3 = 3.1 Max. = 3.4Min. = 1.7,

Use the five-number summary to construct a box plot in the space provided below. a



All the cars observed returned back along the road at some time later in the day and b their travel times between the two sets of traffic lights were recorded on the return journey. The data is displayed in the form of a box plot, as shown below. Use this box plot to determine the median and IQR of the travel times of the cars on the return journey

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- The distribution of travel times on this section of road at peak times is known to be 4 approximately normal with a mean of 3.8 minutes and a standard deviation of 0.4 minutes.
 - Use this information to estimate the percentage of cars whose travelling times are: a
 - i between 3.0 and 4.6 minutes
 - less than 3.4 minutes ii
 - iii between 3.0 and 4.2 minutes
 - A car has a travel time of 5 minutes. b
 - i Determine the standardised travel time (z-score) of this car.
 - What percentage of cars have travel times less than this car? ii
 - A car has a standardised travel time of z = 1.8. What was its actual travel time? Give c your answer rounded to one decimal place.