Formula Sheet

Core – Data analysis

standardised score	$z = \frac{x - \overline{x}}{s_x}$			
lower and upper fence in a boxplot	lower $Q_1 - 1.5 \times IQR$ upper $Q_3 + 1.5 \times IQR$			
least squares line of best fit	$y = a + bx$, where $b = r \frac{s_y}{s_x}$ and $a = \overline{y} - b\overline{x}$			
residual value	residual value = actual value – predicted value			
seasonal index	seasonal index = $\frac{\text{actual figure}}{\text{deseasonalised figure}}$			

Core - Recursion and financial modelling

first-order linear recurrence relation	$u_0 = a, \qquad u_{n+1} = bu_n + c$
effective rate of interest for a compound interest loan or investment	$r_{effective} = \left[\left(1 + \frac{r}{100n} \right)^n - 1 \right] \times 100\%$

Module 1 – Matrices

determinant of a 2×2 matrix	$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}, \qquad \det A = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$
inverse of a 2×2 matrix	$A^{-1} = \frac{1}{\det A} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}, \text{where} \det A \neq 0$
recurrence relation	$S_0 = \text{initial state}, \qquad S_{n+1} = TS_n + B$

Module 4 - Graphs and relations

gradient (slope) of a straight line	$m = \frac{y_2 - y_1}{x_2 - x_1}$
equation of a straight line	y = mx + c

Significant figures vs. Decimal places

- Significant Figures
- → All non- zero values are significant

4.2 (2 sig figs)

→ All zeros in between are significant

40002 (5 sig figs)

- Or, in the case of decimal values: **4**.0002 (5 sig figs)
- \rightarrow **Decimal values**
 - 1. All final zeros after the decimal point are significant

4.200 (4 sig figs)

2. All leading zeros after a decimal point are NOT significant

0.000422 (3 sig figs)

 \rightarrow Terminal zeros don't count UNLESS there is a decimal point at the end

420 (2 sig figs)
420. (3 sig figs)
420. 0 (4 sig figs)

• Decimal places

ightarrow Involves rounding values after the decimal point to however many decimal places

422.347

Round to 2 decimal places : 422 . 35

422.344

Round to 2 decimal places : 422 . 34

ightarrow Money must always be rounded to 2 decimal places or "to the nearest cent"

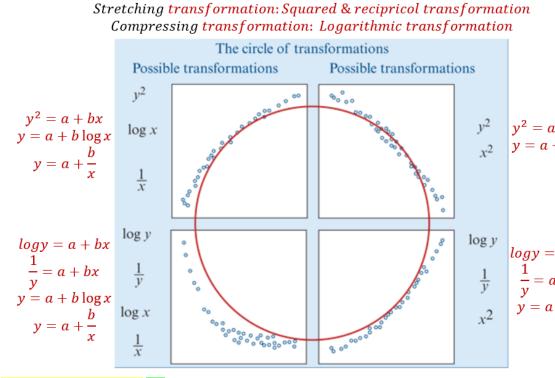
273.245 = 273.25 (to 2 decimal places)

273.245 = 270 (to 2 significant figures)

Topics	Data 1	「ypes <mark>1A</mark>	Display/Ana	lyse Tools	Report/Explain/Interpret/Describe					
Univariate	Categorical	Nominal data	Bar chart, Pie Chart,	Frequency	Mode/ Modal Value					
Data	variables <mark>1B</mark>	Ordinal data	Table <mark>1a</mark> , Segmented	bar chart	Frequency types, Frequency % = $\frac{Count}{Total Count} \times 100\%$					
<mark>All in one</mark> 1.6	Numerical variables <mark>1C</mark>	Discrete data Continuous data	Boxplots <mark>1c</mark> 1.5, Grouped Frequency Tables	Stem plot 1b 1.6, dot plot 1b 1.6 Stem plot 1b 1.6, histogram 1b 1.1, log 1.2 log- histogram1.3	Shape → Centre → Spread → Outliers → 1F	Symmetric Mean \bar{x} 1.4 Standard Deviation S 1G 1.4 68-95-99.7% rule 1H 1.6 1I 1.7 Z-score= $Z = \frac{x - \bar{x}}{S}$ 1I 1.7 $x = \bar{x} + Z * S$	Skewed 1.5 Median M or Q_2 IQR, Range $\begin{bmatrix} 1.6 & Lower Fence = Q_1 - 1.5 * IQR \\ 1.6 & Upper Fence = Q_3 + 1.5 * IQR \\ 1.5 & 5-figure summary: Min, Q_1, Q_2, Q_3, Max \\ IQR=Q_3 - Q_1, Range=Max-Min \end{bmatrix}$			
Bivariate Data	Two categori	cal	Segmented bar chart		Mode/ Modal					
	variables <mark>2A</mark>		frequency table <mark>2a</mark> , p		Frequency typ					
	One categori		Back-to-back stem pl		Shape →	Symmetric	Skewed			
All in one			plots, parallel box plo	ots <mark>2b</mark>	Centre →	<mark>1.4</mark> Mean $ar{x}$	1.5 Median M or Q ₂			
<mark>3.6</mark>					Spread →	Standard Deviation S	IQR, Range			
	The assumptions squares line 1. the data is num 2. the association 3. there are no clear	nerical is linear	Scatterplot 2c 2.1 Explanatory variable residual = actual data value y - residual = $y - \hat{y}$ Nil pattern residual 3.6 relation Curved/ patterned residual relation	Predicted 3.7 value y plot $2f = Linear$ dual plot ≠ linear	Strength \rightarrow Direction \rightarrow Form \rightarrow 3A 3B 3C 2e LSRL y=a+bx 3.1 3.7 3.2 3.7 2e slope $b=\frac{rs_y}{s_x}$ 3.2 3.7 2e y-intercept $a=\overline{y}-b\overline{x}$		f Determination $r^2 \frac{3.1}{3.1}$ be explained / predicted by [EV x].			
Time Series	Features <mark>4A</mark>		Moving smo	-		Seasonal Index S.I. 4D 4.6 4.7	Deseasonalising 4D 4.7			
4A 4E: LSRL 4.1 4.3 4.4 4.5	Trend 🗠 🛌 Cycles 🛄	Moving 3/5 moving mean	g Mean <mark>4B 4.2</mark> 2/4 Moving mean	Jan Feb Mar Apr May Jan 10 12.5 6 5 2.4 19 25	13 7.5 8.5 10 7 15	S.I.= Value for Season Yearly Average Yearly Average= Sum of Season Values No.of Season per year	Deseasonalised Figure = $\frac{Actual Figure}{S.I.}$ = Actual Figure * $\frac{1}{S.I.}$			
	Structure change Outliers	18.1 24.8 26.4	18.1 = 2 = 21.45 24.8 = 21.45 26.4 = 25.6 = 21.45 26.4 = 23.525		Lend /	Correct S.I. = $(\frac{1}{S.I.} - 1) \times 100$ + means \uparrow , - means \downarrow	Actual figure= Deseasonalised Figure * S.I.			

Note: Textbook Summary Notes Section #, Report Instruction Notes #. CAS Instruction Notes #

3D: Data Transformation & 3E 3.3 3.4 3.5 3.6



1D Log Scales & Graphs 1.2

Log (Base 10) Scale

Logarithms

A logarithm, or log, is a power or exponent or index of a number. That is the log of a^b is b. For example the logs of 2^3 , 5^4 , and 10^6 are 2, 3, and 6 respectively.

Log (Base 10) Scale

The log (base 10) scale is based of exponentials of base 10, i.e. $10, 10^2, 10^3, 10^4$. Using the log (base 10) scale allows data ranging over several order of magnitude to be displayed.

Converting Between Forms using the Log (Base 10) Scale

 $\log value = \log_{10}(data value)$

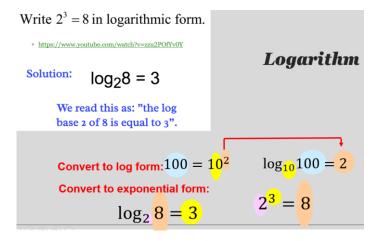
data value $= 10^{\log value}$

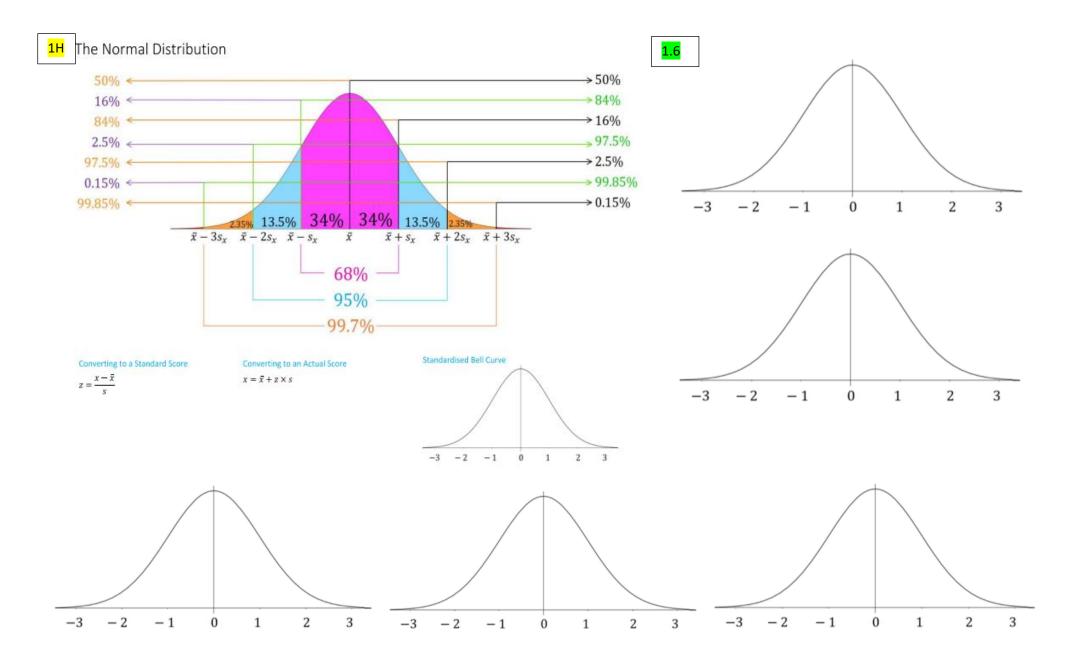
Data Value	0.001	0.01	0.1	10^n	1	10	100	1000
Log Form	$\log_{10} 0.001$	$\log_{10} 0.01$	$\log_{10} 0.1$	$\log_{10} 10^n$	$\log_{10} 1$	$\log_{10} 10$	$\log_{10}100$	$\log_{10}1000$
Log Value	-3	-2	-1	n	0	1	2	3
Exponent Form	10 ⁻³	10 ⁻²	10 ⁻¹	10^n	10 ⁰	10 ¹	10 ²	10 ³

- Best transformation: strongest r/r^2 value Types of transformations:
- Log: compresses the data
- Square: stretches the data
- Reciprocal: compresses values greater than 1, stretches values less than 1.

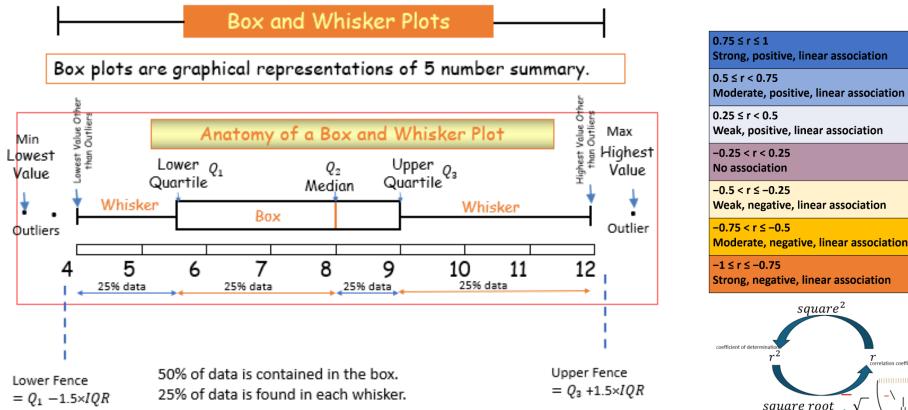
The Effect of Each Transformation:

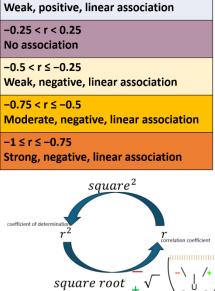
x + bx + bx^2	Type of	Description of Effect:	One Word Description:	Graph of
$+bx^2$	Transformation:			Transformation:
	Squared Transformations (x^2 and y^2)	Spreads out the high x-values relative to the lower x-values and vice versa.	Stretching transformation > x ² stretches high x-values > y ² stretches high y-values	
a + bx a + bx	Log Transformation (Log, and Log,)	Compresses the higher x- values relative to the lower x-values and vice versa	Compressing Transformation	[
$a + bx^2$	Reciprocal Transformations	Compresses larger y- values relative to smaller y-values and vice versa	Stretching and Compressing Transformation	





1E: The Box Plot 1.6





Data Summary Notes

1A: Types of data

Categorical: characteristics/qualities

- Nominal: grouped according to characteristics
- Ordinal: can be grouped and ordered

Numerical: numbers/quantities

- Discrete: whole numbers, can be counted
- Continuous: is measured

1B: displaying categorical data

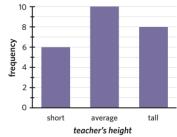
Count frequency: number of times the category appears in the data

Percentage frequency: $\frac{count \ frequency}{total \ count} \times 100$ Mode: most frequently occurring value or category Frequency Table:

teacher's	freq	uency		
height	number	%		
short	6	25.0		
average	10	41.7		
tall	8	33.3		
total	24	100.0		

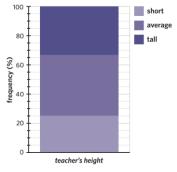
Bar chart:

• Must have gaps between bars



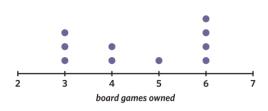
Segmented bar chart:

- Can be count or percentage frequency
- Must have a key



<u>1C: Displaying Numerical data</u> Dot plot

- Discrete data
- Small data sets



Stem and leaf plot

- Needs a key
- Can have class intervals (splitting the stem in two if it is really large)

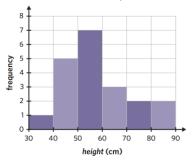
	No intervals					W	ith	cla	ass	int	erv	/als	s of 5	5		
Key:	Key: 1 2 = 1.2			ŀ	(ey:	1	2 =	= 12	2							
1	3	3	4	6	8				0	1	1	2	3	4		
2	0	4	9						0	5	6	6	8	8	9	
3	1	1	1	4	5	8			1	2	3	3				
4	2								1	6	7	7	8	9	9	

Grouped frequency tables

height (cm)	frequency					
neight (cm)	number	%				
30-<40	1	5				
40-<50	5	25				
50-<60	7	35				
60-<70	3	15				
70-<80	2	10				
80-<90	2	10				
total	20	100				

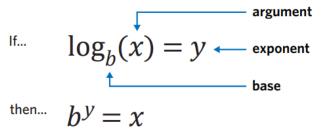
Histogram:

- Continuous data
- Intervals no gaps between bars
- No gaps between bars
- X-axis markers are always a whole number

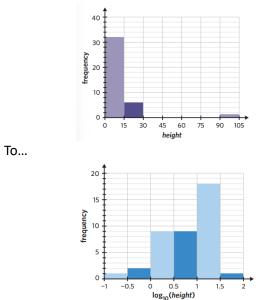


1D: Log scales and graphs

- Log scales are used to compress data that has a large range, making it more even and able to be displayed on the same set of axes.
- The base is always 10
- When undoing the log scale do ten to the power of the scale (eg. $10^{2.2} = 158.5$)



From...

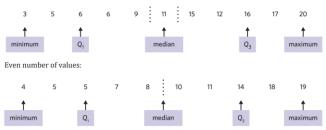


1E: the five-number summary and boxplots

5 number summary:

- Minimum: smallest value in data set
- Q1: median of the lower half
- Median: middle value in an ordered data set
- Q3: median of the upper half
- Maximum: largest value in data set

Odd number of values



Spread: refers to how variable the data set it Range = maximum – minimum

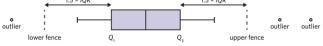
Interquartile range: measure of spread of the middle 50% of a data set. Accurate measure of spread when outliers are present.

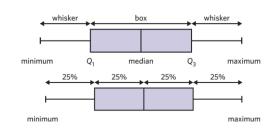
$IQR = Q_3 - Q_1$

Outliers: values which fall outside of what is 'normal'. Outliers are still the minimum and maximum value! **Fence:** defines the boundary of what is an outlier. If a value is less than the lower fence or greater than the upper fence it is considered to be an outlier.

$$lower fence = Q_1 - (1.5 \times IQR)$$

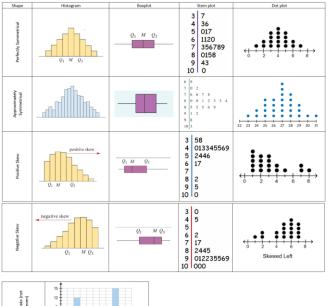
$$upperfence = Q_3 + (1.5 \times IQR)$$

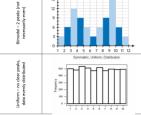




1F: describing numerical data

- Shape: is the data symmetrical, skewed or have any outliers?
- Centre: What is the median value?
- Spread: What is the range and IQR?





1G: Standard deviation

Population: the entire group is used to collect data. Sample: smaller subset of the population (this is usually what is used).

Mean: measure of centre – the AVERAGE. $\overline{\chi}$

 Calculated by adding all the data values together and then dividing by the number of values.

 $\bar{x} = \frac{\Sigma x}{n}$, where Σx is the 'sum of all values', and *n* is the number of values in the data set.

Standard deviation: measure of spread based on the average deviation of each data point compared to the mean. It can be calculated by hand but please use CAS.

$$s_x = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}}$$

Boxplots:

1H: The Normal Distribution

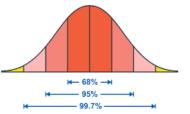
Normal Distribution: is a symmetrical (or

approximately) numerical data set centred around the mean.

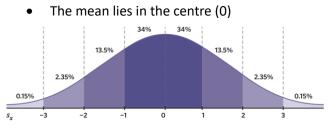
- Bell shaped
- Mean and median are equal

68-95-99.7% rule:

- 68% of the data lies within one standard deviation of the mean
- 95% of the data lies within two standard deviations of the mean
- 99.7% of the data lies within three standard deviations of the mean



The bell curve can be broken into each section:



11: z-scores

Standardised score:

- Z-score
- Measure of the number of standard deviations between the mean and a data value
- Each data value is an 'actual score'
- Positive = above mean, negative = below mean, zero = equal to mean

 $z = \frac{x - \overline{x}}{s_x}$

- *z* is the standardised score
- *x* is the actual score
- \overline{x} is the mean
- s_x is the standard deviation

Actual score:

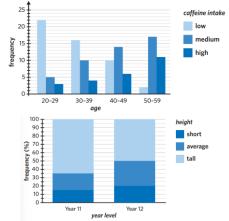
 $x = \overline{x} + (z \times s_{r})$

2A: association between 2 variables

Two-way frequency table:

- Columns = EV, Rows = RV
- Percentage frequency is used for greater accuracy when making comparisons if sample sizes are different

Grouped and segmented bar charts:

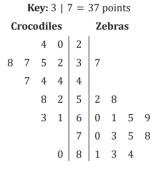


Describing the association between two variables:

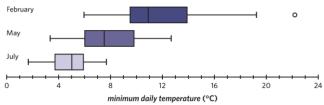
- Whether or not an association between the two variables exists
- Appropriate percentages to support findings

2B: association between numerical and categorical variables

Back to back stem plot



Parallel boxplot



• Making comparisons: refer to 1F and compare shape, centre and spread of the two categories

2C: association between two numerical variables

Response variable: RV, may be explained or predicted by changes in the explanatory variable.

Explanatory variable: EV, used to explain or predict the changes observed in the response variable.

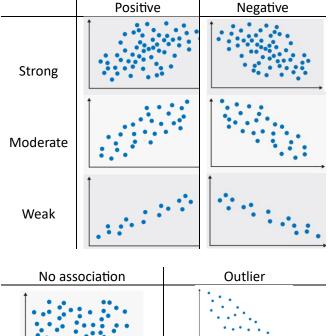
• 'EV explains the RV'

Scatterplots:

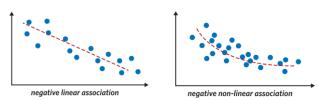
EV = x axis, RV = y axis

Describing relationship/analysing scatterplots:

- Strength: how close the data points are together
- Direction: positive or negative



• Form: linear (straight) or non-linear (curved)



2D: Correlation and causation

Pearson's correlation coefficient (r): numerical value that determines strength and direction between two numerical variables, assuming:

- Data is linear
- Data is numeric
- No outliers present

$0.75 \le r \le 1$	Strong, positive, linear association
$0.5 \le r < 0.75$	Moderate, positive, linear association
$0.25 \le r < 0.5$	Weak, positive, linear association
-0.25 < r < 0.25	No association
$-0.5 < r \leq -0.25$	Weak, negative, linear association
$-0.75 < r \leq -0.5$	Moderate, negative, linear association
$-1 \le r \le -0.75$	Strong, negative, linear association

Correlation and Causation: just because two variables have a high correlation, it doesn't mean that one causes the change in the other. Some explanations:

 Common response: a third variable that is the likely cause of correlation, acting on both variables. Eg. Number of people wearing sunscreen and feinting → the sunscreen isn't causing people to feint... the third variable would be temperature. This is common cause as temperature affects **both** variables.

- Confounding variable: external variable that can also produce a change to the RV. Eg. Plant height and water intake. Water intake does effect plant height (RV) but so does sun, soil quality, buys, season, temperature...
- **Coincidence:** two variables correlate but have no relation to each other. Pure chance. No logical explanation.

3A: fitting a least squares regression line

Least squares regression line (LSRL): is the line which creates the minimum sum of the squares of residuals. There are assumptions:

- Data is numerical
- The relationship between variables is linear
- There are no clear outliers present

The line is used to show the general trend in the data and is given by the equation:

$$y = a + bx$$

Intercept Slope

Determining LSRL from a graph: Find the intercept (a) and the slope (b).

- Intercept: read directly from the graph when the EV is 0
- Slope: choose two points on the line that you can clearly ready the coordinates. Use the rule:

$$b = \frac{rise}{run} = \frac{y_2 - y_1}{x_2 - x_1}$$

Calculating the LSRL from summary statistics:

$$b = r \times \frac{s_y}{s_x}$$
$$a = \overline{y} - b\overline{x}$$

• *a* is the *y*-intercept

- *b* is the gradient
- *r* is Pearson's correlation coefficient
- \bar{x} is the mean of the explanatory variable (*x*)
- \overline{y} is the mean of the response variable (y)
- s_x is the standard deviation of the explanatory variable (x)
- s_v is the standard deviation of the response variable (y)

Drawing the LSRL on a graph: Sub in the first value on the x-axis and the last value on the x-axis into the equation. Plot the two points, join the line using a ruler.

3B: Interpreting LSRL: use the following statements, fill in EV and RV and values of a and b. y-intercept: when the EV is 0, the RV is a. Slope: for every one-unit increase in the EV, the RV increases/decreases by b. (If b is positive, increases, if b is negative, decreases) **Making predictions:** the LSRL can be used to predict the value of the RV from the EV.

Interpolation: predicting within the range of data. **Extrapolation:** predicting outside the range of data. Less reliable.

How to predict: sub the EV value that you are predicting for into the LSRL equation to predict the RV.

3C: Performing a regression analysis:

Coefficient of determination (r²): calculated by squaring the r value. It is turned into a percentage (×100) then interpreted. Use the statement by inputting the variable names and percentages:

• **r²** % of the variation in the **RV** can be explained by the variation in the **EV**. The remaining % can be explained by other factors.

Residuals: residuals are the vertical distances between the data point and the LSRL.

residual = actual data value - predicted data value

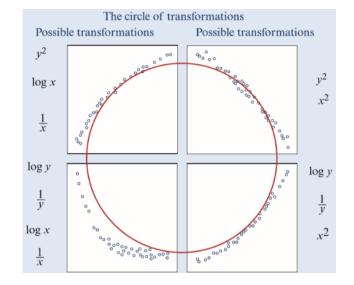
- Actual value: found in the question/table of data
- Predicted value: must use the LSRL to predict the RV from the EV
- Positive residual = data point above LSRL, negative residual = data point below LSRL, zero residual = data point on the LSRL.

Residual plots:

	-			
Random scattering of	Clear curved pattern in			
points in the residual	the residual plot, does			
plot, supports the	not support the			
assumption of linearity	assumption of linearity			
	residual -2 -2 -2 -2 -2 -2 -2 -2 -2 -2			

3D: Data Transformations: You shouldn't perform a linear regression analysis for data that is nonlinear. Therefore, nonlinear data is transformed.

- Transformation linearise data so that regression analysis can be performed accurately.
- Match the nonlinear scatterplot with one in the diagram to help you determine the best transformation.
- Best transformation: strongest r/r² value Types of transformations:
 - Log: compresses the data
 - Square: stretches the data
 - Reciprocal: compresses values greater than 1, stretches values less than 1.



<u> 3E: Data transformations – applications</u>

LSRL: once you have transformed your data you must create a new LSRL equation and include the transformation in the rules.

Eg. From y = -16.14 + 9.39x

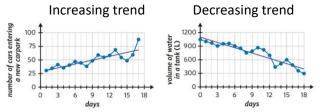
То

 $y = -0.73 + 1.05x^2$

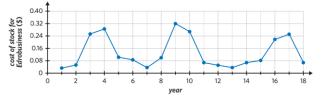
Making predictions: the limits of extrapolation are still present. When calculating, use solve as this will undo the transformation for you.

<u>4A: Time series data and their graphs</u>

Trends: general upwards (increasing) or downwards (decreasing) movement over time. Trend lines can be fitted directly to trends. There can be multiple trend lines.



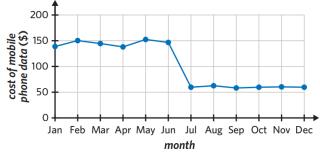
Cycles/cyclical variation: periodic movements over a period greater than 1 year. Peaks of cycles occur at approximately the same intervals, cycles can have a period which changes slightly between peaks.



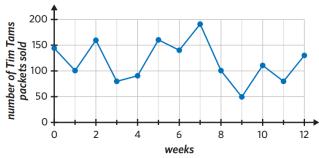
Seasonality: cyclical variation within a calendarrelated period (week, month, quarter). A seasonal time series plot has regular peaks and troughs that occur at the same time each period and the length of the period must be a year or less.



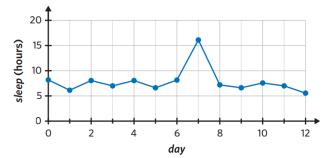
Structural Change: When an established pattern is suddenly altered. The graph then continues on the same level post structural change.



Irregular fluctuations: random variations that cannot be explained by trend, seasonality, cycles or structural change.



Outliers: stands out from the general body of data. It then returns to follow the original pattern/trend



<u>4B: Smoothing – moving means</u>

Smoothing: evens out fluctuations to help identify any underlying trends

- Only smooth the RV
- The larger the mean smooth, the more effective (5 more effective than 3)

3 mean: use 3 values and find the mean

5 mean: use 5 values and find the mean

• Always centred around the value you are trying to smooth

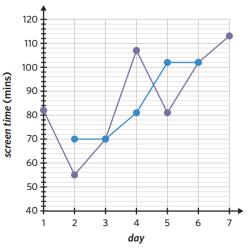
day	temp. (°C)	calculation	three-mean smoothed <i>temperature</i> (°C)
Mon	24	-	-
Tue	27	$\frac{24+27+21}{3}$	24
Wed	21	$\frac{27+21+18}{3}$	22
Thu	18	$\frac{21+18+15}{3}$	18
Fri	15	$\frac{18+15+15}{3}$	16
Sat	15	$\frac{15+15+12}{3}$	14
Sun	12	-	-

Smoothing with centring: an additional step when smoothing with an even number of points. Finding the mean of two non-centred means.

day	temp. (°C)	before centring	after centring
Mon	24		-
		$\frac{24+27}{2} = 25.5$	
Tue	27		$\frac{25.5 + 24}{2} = 24.75$
		$\frac{27+21}{2} = 24$	
Wed	21		$\frac{24+19.5}{2} = 21.75$
		$\frac{21+18}{2} = 19.5$	
Thu	18		-

<u> 4C Smoothing – moving medians</u>

- Smoothed directly on the graph
- Median smoothing only uses and odd number of points
- Smooth the RV



<u>4D: Seasonal adjustments:</u>

- Seasonal fluctuations exist.
- Seasonal indices (SI) are used to deseasonalise the data to minimise the effects of seasonality. This allows trends to be more easily observed.

Rules

1. Seasonal index $(SI) = \frac{value \ for \ season}{seasonal \ average}$

2. Seasonal average $(SA) = \frac{sum of all seasons}{number of season}$

3. Deseasonalised figure (DS) = $\frac{value \ for \ season}{seasonal \ index}$

4. Reseasonalising data:

value for season = deseasonalised figure \times seasonal index

```
    A negative %: (season) is below the seasonal average by ____%
    A positive %: (season) is above the seasonal average by ____%
    Correcting for seasonality:
```

 $(\frac{1}{seasonal\ index} - 1) \times 100 = ___{\%}$

- A negative %: To correct (season) for seasonality, (unit) need to be decreased by %
- A positive %: To correct (season) for seasonality, (unit) need to be increased by _____%

Notes:

- The sum of the seasonal indices is equal to the number of seasons (if you are working with months of the year there are 12 seasons and therefore the seasonal indices will sum to 12)
- If there were no fluctuations, the seasonal average is 1

4E: Time series data and LSRL modelling:

Trend lines: can be fitted to time series plots if there appears to be an increasing or decreasing trend.

- The LSRL is used
- If seasonality is present, data needs to be deseasonalised first before fitting the LSRL to the deseasonalised values

Forecasting: making a prediction for the future

 You need to re-seasonalise the value if the prediction was made from a deseasonalised LSRL

1.1 Constructing a histogram from raw data

CAS 1: How to construct a histogram using the TI-Nspire CAS

 Display the following set of 27 marks in the form of a histogram.

 16
 11
 4
 25
 15
 7
 14
 13
 14
 12
 15
 13
 16
 14

 15
 12
 18
 22
 17
 18
 23
 15
 13
 17
 18
 22
 23

 Steps

- 1 Start a new document by pressing [em + ℕ (or @mo>New. If prompted to save an existing document, move the cursor to No and press [enter]
- 2 Select Add Lists & Spreadsheet. Enter the data into a list named marks.
 - a Move the cursor to the name cell of column A and type in *marks* as the list variable. Press [mter].
 - b Move the cursor down to row 1, type in the first data value and press enter. Continue until all the data have been entered. Press enter after each entry.

16

4

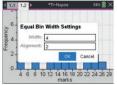
15

- 3 Statistical graphing is done through the Data & Statistics application. Press en + 1 (or alternatively press en doc-) and select Add Data & Statistics.
 - a Press the enter (or click on the Click to add variable box on the x-axis) to show the list of variables. Select marks. Press enter to paste marks to that axis.
 - A dot plot is displayed as the default. To change the plot to a histogram, press mem>Plot Type> Histogram. The histogram shown opposite has a column (or bin) width of 2, and a starting point (alignment) of 3. See Step 5 below for instructions on how to change the appearance of a histogram.
- 4 Data analysis
 - a Move the cursor over any column; a ⊕₁ will appear and the column data will be displayed as shown opposite.
 - **b** To view other column data values, move the cursor to another column.

Note: If you click on a column, it will be selected.

- Hint: If you accidentally move a column or data point, etc. + esc. enter will undo the move.
 Change the histogram column (bin) width to 4 and the starting point to 2.
 - a Press [cfr] + [menu] to access the context menu as shown (below left). Hint: Pressing [cfr] + [menu] [enter] with the cursor on the histogram gives you a context menu that
 - relates only to histograms. You can access the commands through memo>Plot Properties b Select Bin Settings>Equal Bin Width.
 - c In the settings menu (below right) change the Width to 4 and the Starting Point (Alignment) to 2 as shown. Press [mttr].

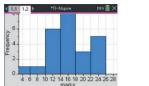


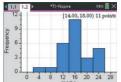


(13.000, 15.000) 6 p

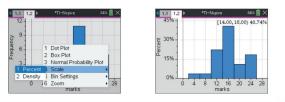
14 16 18

d A new histogram is displayed with column width of 4 and a starting point of 2 but it no longer fits the window (below left). To solve this problem, press err. + memu>Zoom>Zoom>Data and errer to obtain the histogram as shown below right.





6 To change the frequency axis to a percentage axis, press etr + memp>Scale>Percent and then press enter.



1.2 Working with logarithms

Example 12 Using a CAS calculator to find logs

- **a** Find the log of 45, correct to two significant figures.
- **b** Find the number with log equal to 2.7125, correct to the nearest whole number.

Explanation

- a Open a calculator screen, type log (45) and press [enter]. Write down the answer correct to two significant figures.
- b If the log of a number is 2.7125, then the number is 10^{2.7125}.
 Enter the expression 10^{2.7125} and press [enter].

Write down the answer correct to the nearest whole number.

€ 1.1 ▶	*TI-Nspire	DEG 🗐	×
log (45)		1.65321	1
10 ^{2.7125}		515.822	
I.			
a log 45	= 1.65		
a log 45	= 1.65 = 1.7 (to 2	sig. figs)	
U		0.01	
	= 1.7 (to 2		st

1.3 Constructing a histogram with a log scale

CAS 2: Using a TI-Nspire CAS to construct a histogram with a log scale

The v	weights	of 27	animal	specie	es (in	kg)	are 1	record	ed below.	
					-					

l	1.4	470	36	28	1.0	12000	2600	190	520	
l	10	3.3	530	210	62	6700	9400	6.8	35	
l	0.12	0.023	2.5	56	100	52	87 000	0.12	190	
l	Constr	uct a hist	ogram	to dis	nlay th	e distribu	tion.			

a of the body weights of these 27 animals and describe its shape

b of the log of the body weights of these animals and describe its shape.

Steps

Statistics

plot is displayed.

Type>Histogram.

- **1 a** Start a new document by pressing etri + N.
- b Select Add Lists & Spreadsheet.Enter the data into a column named weight.

Click on the Click to add variable on the

x-axis and select the variable weight. A dot

2 a Press [tr] +] and select Add Data &

b Plot a histogram using menu>Plot

c Describe the shape of the distribution.

3 a Return to the Lists & Spreadsheet screen.

4 a Plot a histogram using a log scale. That is,

Width and set the column width (bin) to 1 and alignment (start point) to -2 and use menu>Window/Zoom>Zoom-Data to rescale

Note: Use menu>Plot Properties>Histogram Properties>Bin Settings>Equal Bin

plot the variable logweight.

c Move the cursor to the formula cell below the

logweight heading. Type in = log(weight).

Press enter to calculate the values of logweight.

b Name another list logweight.

1.1 TT-Mapre cu () A weight C D 1 1.4 C 2 470 3 3 36 4 4 28 5 5 1.1 C 11.1 1.2 TT-Mapre 24 C 21 1.4 C 21 C 21 C 24 C 24 C 24 C 24 C 24 24 30 31 24 0 0 0 0 0

Shape: positively skewed with outliers

 Initial
 Th-Napic
 C60
 X

 A weight
 Elogyet_C
 D
 D

 Initial
 1.4
 0.146128
 D
 D

 2
 470.0
 2.6721
 3
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 1.5563
 D

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 1.44716
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 5
 legweight=log
 10
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Shape: approximately symmetric

b Describe the shape of the distribution.

1.4 Calculating the standard deviation

CAS 3: How to calculate the mean and standard deviation using the TI-Nspire CAS

The following are the heights (in cm) of a group of women.

176 160 163 157 168 172 173 169

Determine the mean and standard deviation of the women's heights. Give your answers correct to two decimal places.

1.3 Constructing a histo CAS 2: Using a TI-Nspiro The weights of 27 animal spec

Steps

- 1 Start a new document by pressing etrl + N.
- 2 Select Add Lists & Spreadsheet.
- Enter the data into a list named *height*, as shown.
 3 Statistical calculations can be done in either the Lists & Spreadsheet application or the Calculator application (used here).

Press er + 1 and select Add Calculator.

- a Press menu>Statistics>Stat Calculations>One-Variable Statistics. Press enter to accept the
- Num of Lists as 1.
 i To complete this screen, use the b arrow and enter to paste in the list name *height*.
 - ii Pressing enter exits this screen and generates the results screen shown opposite.

=	_				
1	176				
2	160				
3	163				
4	157				
5	168				
AL I	76				4 3
1.1	1.2 D	*TI-Nsp Statist		(000 🗐 🔿
1.1 Or	1.2 D e-Variable X1 L	Statist	ics		•
1.1 Or	1.2 e-Variable X1 L Frequency L	Statist ist: heig ist: 1	ics		· ()
1.1 Or	1.2 xi L X1 L Category L	Statist ist: heig ist: 1 ist:	ics		•
1.1 Or	1.2 e-Variable X1 L Frequency L	Statist ist: heig ist: 1 ist:	ics ght		•
1.1 Or	1.2 xi L X1 L Category L	Statist ist: heig ist: 1 ist:	ics) () () () () () () () () () (



4 Write down the answers to the required degree of accuracy (i.e. two decimal places).

is $\bar{x} = 167.25$ cm and the standard deviation is s = 6.67 cm.

28

21

0 5 10 15 20 25 30 35 40 45 50

1.1 1.

Notes: **a** The sample standard deviation is \mathbf{sx} .

b Use the ▲ ▼ arrows to scroll through the results screen to obtain values for additional statistical values.

1.5 Constructing a boxplot with outliers

CAS 4: How to construct a boxplot with outliers using the TI-Nspire CAS $% \left({{\mathbf{TI}}_{\mathbf{T}}} \right)$

43 31 30 34 48 36 35 23 24

Steps

- **1** Start a new document by pressing **ctrl**+**N**.
- 2 Select Add Lists & Spreadsheet. Enter the data into a list called *marks* as shown.
- Statistical graphing is done through the
 Data & Statistics application.
 Press end + 1 and select Add Data & Statistics.

Note: A random display of dots will appear – this indicates that list data are available for plotting. Such a dot is not a statistical plot.

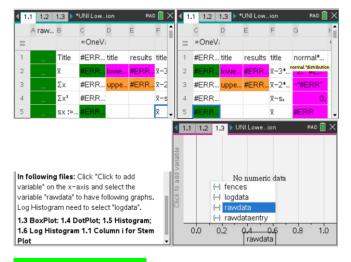
- a Click on the Click to add variable on the x-axis and select the variable marks. A dot plot is displayed by default as shown opposite.
- b To change the plot to a boxplot press memu>Plot Type>boxplot. Your screen should now look like that shown opposite.
- 4 Data analysis
- Key values can be read from the boxplot by moving the cursor over the plot or using [mem]>Analyze>Graph Trace.

Starting at the far left of the plot, we see that the:

- minimum value is 3 (an outlier)
- first quartile is 23 ($Q_1 = 23$)
- median is 30 (**Median** = **30**)
- third quartile is $35 (Q_3 = 35)$
- maximum value is 48.

1.6 Using "UNI Lower Upper Fences Normal Distribution" template

1.1 1.2 1.3 ► UNI Loweion RAD	×	1.1 1.2 1.3 ▶ UNI Lowe_ion 1	rad 📘 🗡
Fences Either ENTER RawData into column	î	Normal Distribution Either ENTER	
a of 1.1	I	RawData into column a of 1.1	
Or	I	Or	
Enter Q1 into C9	IJ	Enter x into C2	- 1
Enter Q3 into C11		Enter s _x into C5	
ENTER		ENTER	



1.7 Using "Z Score" template

Enter all known data into green boxes as indicated on the column a of data title, results will come out in the coloured area



2.1 Constructing a scatterplot Grouped Bar Graph: Menu 2 9; Parallel Box plot Menu 2 5; Regression line: Menu 4 6 2; Line Equation: Menu 4 6 2 (graph), Menu 4 1 4 (Spreadsheets), Menu 6 1 4 (Calculator)

12 15 15

17

14 16

CAS 1: How to construct a scatterplot using the TI-Nspire CAS

6 6 12 13

Construct a scatterplot for the set of test scores given below. Treat *test 1* as the explanatory (i.e. *x*) variable.

6 8 5

9

Test 1 Test 2 Steps

10 18 13

12

20 11

1 Start a new 1,1 1,2 document by pressing etri + N 12 2 Select Add Lists & 13 11 Spreadsheet Enter the data into lists named test1 and test2. 3 Press [tr] +] and select Add Data & Statistics. 4 a Click on Click to add variable on the x-axis and select the explanatory variable test1. b Click on Click to add variable on the y-axis and select the response variable test2. A scatterplot is displayed. The plot is scaled automatically.

2.2 c	alcu	latin	g the	cori	relatio	n coe	fficie	nt r usiı	ng t	the forr	nula
How	to c	alcul	ate t	he c	orrela	tion c	oeffi	cient us	ing	; the for	rmula
Use t	he for	mula t	to cale	culate	the corr	elation	coeffi	cient, r, f	or t	he follow	ing data.
x	1	3	5	4	7			$\bar{x} = 4$,	S _x :	= 2.236	
у	2	5	7	2	9			$\bar{y} = 5$,	s_y :	= 3.082	
Give	the va	lues r	ounde	d to t	wo deci	mal pla	ices.				
Step	S										
1 W	rite do	own th	e valu	ies of	the mea	ins,		$\bar{x} = 4$	1 s,	x = 2.236	
sta	andard	l devia	tions	and <i>n</i>				$\bar{y} = 5$	5 s _y	= 3.082	<i>n</i> = 5
		table			own		x	$(x - \bar{x})$	у	$(y - \bar{y})$	$(x-\bar{x}) \times (y-\bar{y})$
		to cal $(v - \bar{v})$		e			1	-3	2	-3	9
	(x - x))(y – y					3	-1	5	0	0
							5	1	7	2	2
							4	0	2	-3	0
							7	3	9	4	12
							Sum	0		0	23
							∴ <u>∑</u> ($(x-\bar{x})(y-\bar{x})$	- <u>ÿ</u>)	= 23	
Su	ibstitu		appro	priate	values					$\frac{(x-\bar{x})(y}{(n-1)s_x}$	
ro	unding	g the a	inswei	r to tw	o decin	nai plac	ces.	∴ <i>r</i> =	(5	$(-1) \times 2$	$\frac{23}{236 \times 3.082}$

2.3 Using "r value by formula" template to calculate the correlation oefficient r using the formula

= 0.834... = 0.83 (2 d.p.)

74

75 182 167 62

63 178

184

0

-84.823 +0.86729-3

164 168 172 176 180 184

173 64

74

68

62

Enter all data in green area and answer will come in pink box

٩	1.	.1 🕨	ß	r value b			RAD 📘	×
Γ		Αx	ву	r value b	y formula	E	F	î
	=							ľ
	1	-	_	title				
	2	_	_	n	_	r		
	3	_	_	x	-			
	4	_	_	ÿ	1			
	5	_		Sx	_			•
		-						_

3.1 Determining the equation of the least squares regression Line

CAS 1: How to determine and graph the equation of a least squares regression line using the TI-Nspire CAS

The following data give the height (in cm) and weight (in kg) of 11 people.

Height (x)	177	182	167	178	173	184	162	169	164	170	180
Weight (y)	74	75	62	63	64	74	57	55	56	68	72

Determine and graph the equation of the least squares regression line that will enable weight to be predicted from height. Write the intercept and slope rounded to three significant figures.

Steps

- 1 Start a new document by pressing etri + N.
- 2 Select Add Lists & Spreadsheet. Enter the data into lists named height and weight, as shown.
- 3 Identify the explanatory variable (EV) and the response variable (RV).

EV: height RV: weight

Note: In saying that we want to predict weight from height, we are implying that height is the EV.

4 Press [tr] +] and select Add Data & Statistics Construct a scatterplot with height (EV) on the horizontal (or x-) axis and weight (RV) on the vertical (or y-) axis.

Press menu>Settings and click the Diagnostics box. Select OK to activate this feature for all future documents. This will show the coefficient of determination (r^2) whenever a regression is performed.

5 Press menu>Analyze>Regression>Show Linear (a + **bx)** to plot the regression line on the scatterplot. Note that, simultaneously, the equation of the regression line is shown on the screen. The equation of the regression line is:

 $weight = -84.8 + 0.867 \times height$

The coefficient of determination is $r^2 = 0.723$, rounded to three significant figures.

3.2 Conducting a regression analysis using data

e CAS

5.2 Conducting a rep	gres	sior	1 an	alys	is us	sing	dat	a			
CAS 2: How to condu	ict a	reg	res	sion	ana	lysi	s us	ing t	he T	I-Ns	spire CAS
This analysis is concerned years) and birth rate (in bi									een li	ife ex	pectancy (in
Birth rate	30	38	38	43	34	42	31	32	26	34	
Life expectancy (years)	66	54	43	42	49	45	64	61	61	66	
Steps Write down the explan. (EV) and response vari the variable names <i>birt</i>	able	(RV)	. Use		EV: RV:						
2 Start a new document b ctrl + N.	oy pro	essin	g		< 1.1 A	▶ birth	B life	Nspire C		DEG (
Select Add Lists & Spre	adsl	neet.			1	30	-	66			
Enter the data into the and <i>life</i> , as shown.	lists 1	name	d bir	th	2 3 4 5 A1 3	38 38 43 34	3	54 43 42 49		4	-
3 Construct a scatterplot the nature of the relation life expectancy and bir	nshij	bet			 1.1 66 - 60 - 48 - 42 - 	•	•	•	• • 36 38	DEO (0 40 42	• 44
4 Describe the associatio scatterplot. Mention di					relati	ionsh	ip be	twee	n life		ectancy and
strength and outliers.		f di -	1		_				e no c	obvio	us outliers.
5 Find and plot the equat squares regression line Note: Check if Diagnost using memi>Settings.	and	r ² val	lue.		 ■ 1.1 66 - 60 - 48 - 48 - 42 - 	• y = 10 r ² = 0.	05.373+		36 38	40 42	×
6 Generate a residual plo linearity assumption. Use @n + ◄ (or click of to return to the scatterp To hide the residual plo	on the lot. ot pre	e pago			41.1 60- 52- 44- 8- 0- 0-	r ² = 0.	~	32 34 birti		40 42	
menu>Analyze>Residua Residual Plot.	u5>H	ide			Res -8-	0		0	0	•	0
7 Use the values of the in slope to write the equat		-			Regr	essio	-	ation			

slope to write the equation of the least squares regression line. Also write the values of r and the coefficient of determination.

$life = 105.4 - 1.445 \times birth$

Correlation coefficient: r = -0.8069Coefficient of determination: $r^2 = 0.651$

3.3 Perform a squared transformation

(CAS 1: Using the TI-Nspire CAS to perform a squared transformation													
1	The table shows the height (in m) of a base jumper for the first 10 seconds of her jump.													
	Time	0	1	2	3	4	5	6	7	8	9	10		
	<i>Height</i> 1560 1555 1540 1516 1482 1438 1383 1320 1246 1163 1070													
١.	Constr	net a se	atternl	ot displ	aving h	eioht (1	he RV)	agains	t time (the EV)			

- **b** Apply an *x*-squared transformation and fit a least squares line to the transformed data. **c** Use the regression line to predict the height of the base jumper after 3.4 seconds.
- Steps



- 2 Select Add Lists & Spreadsheet.
- Enter the data into lists named time and height, as shown.
- 3 Name column C as *timesq* (short for 'time squared'). 4 Move the cursor to the formula cell below *timesq*. Enter the expression = $time^2$ by pressing (=), then typing timeA2. Pressing enter calculates and displays the values of timesq.
- 5 Press etri + 1 and select Add Data & Statistics. Construct a scatterplot of height against time. Let time be the explanatory variable and height the response variable. The plot is clearly non-linear.



1 2 3 4 5 6 7 8 9 10

- 6 Press etri + 1 and select Add Data & Statistics. Construct a scatterplot of height against time2. The plot is now linear.
- 7 Press menu>Analyze>Regression>Show Linear (a + bx) to plot the line on the scatterplot with its equation. Note: The x in the equation on the screen corresponds to the transformed variable time2
- 8 Write down the regression equation in terms of the variables height and time².
- 9 Substitute 3.4 for *time* in the equation to find the height after 3.4 seconds.

3.4 Applying the log transformation

CAS 2: Using the TI-Nspire CAS to perform a log transformation

125

4 1.1

140

1250

110

 $height = 1560 - 4.90 \times 3.4^2 = 1503 \text{ m}$

79.2

77.4

78.8

81.5

74.9

72.0

77.9

70.3

73.0

68.6

 $height = 1560 - 4.90 \times time$

The table shows the <i>lifespan</i> (in years) and <i>GDP</i> (in dollars)	Lifespan	GDP
of people in 12 countries. The association is non-linear. Using the log x transformation:	80.4	36 0 32
 linearies the date and fit a representation line to the 	79.8	34 484

- linearise the data, and fit a regression line to the transformed data (GDP is the EV)
- write its equation in terms of the variables *lifespan* and GDP rounded to three significant figures.
- use the equation of the regression line to predict the lifespan in a country with a GDP of \$20 000, rounded to one decimal place.

Steps

- 1 Start a new document by pressing etr + N.
- 2 Select Add Lists & Spreadsheet. Enter the data into lists named lifespan and gdp.
- **3** Name column C as *lgdp* (short for log (*GDP*)). Now calculate the values of log (GDP) and store them in the list named lgdp.
- 4 Move the cursor to the formula cell below the *lgdp* heading. We need to enter the expression = log(gdp). To do this, press (=) then type in log(gdp). Pressing enter calculates and displays the values of lgdp.
- 5 Press ett + 1 and select Add Data & Statistics. Construct a scatterplot of lifespan against GDP. Let GDP be the explanatory variable and lifespan the response variable. The plot is clearly non-linear.
- 6 Press and + I and select Add Data & Statistics. Construct a scatterplot of lifespan against log(GDP). The plot is now clearly linear.
- 7 Press menu>Analyze>Regression>Show Linear (a + bx) to plot the line on the scatterplot with its equation. Note: The x in the equation on the screen corresponds to the transformed variable log (GDP).
- 8 Write the regression equation in terms of the variables lifespan and log (GDP).
- **9** Substitute 20 000 for *GDP* in the equation to find the lifespan of people in a country with GDP of \$20 000.

lifespan	B gdp	C	D		1
80.4	36032.				
79.8	34484.				
79.2	26664.				
77.4	41890.				
78.8	26893.				١.
	80,4 79,8 79,2 77,4	79.8 34484. 79.2 26664. 77.4 41890.	80.4 36032. 79.8 34484. 79.2 26664. 77.4 41890.	80.4 36032. 79.8 34484. 79.2 26664. 77.4 41890.	80.4 36032. 79.8 34484. 79.2 26664. 77.4 41890.

26 6 6 4

41 890

26 893

25 592

7454

1713

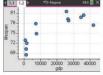
7073

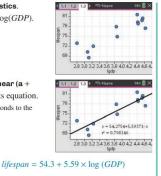
1 1 9 2

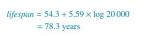
631

1 302









3.5 Applying the reciprocal transformation

CAS 3: Using the TI-Nspire CAS to perform a reciprocal transforma-

The table shows the length (in cm) and width (in cm) of eight sizes of sticky labels.

Length	6.8	5.6	4.6	4.2	3.5	4.0	5.0	5.5
Width	1.8	2.0	2.5	3.0	3.5	2.6	2.0	1.9
Using the 1	/v trans	formati	on.					

- Interview Interv • write its equation in terms of the variables *length* and *width*
- use the equation to predict the width of a sticky label with a length of 5 cm.

Steps

- 1 Start a new document by pressing etrl + N. 2 Select Add Lists & Spreadsheet
- Enter the data into lists named length and width 3 Name column C as recipwidth (short for 1/width). Calculate the values of recipwidth Move the cursor to the formula cell below the recipwidth heading. Type in =1/width. Press enter to calculate the values of recipwidth.
- 4 Press etri + 1 and select Add Data & Statistics. Construct a scatterplot of width against length. Let length be the explanatory variable and width the response variable. The plot is clearly non-linear.
- 喜 2.6. 2.0 4.8 5.2 5.6 6.0 6.4 6.8 3.2 3.6 4.0 1.1 1 0.54 10.46 0.38 0.30 3.2 3.6 4.0 4.4 4.8 5.2 5.6 6.0 6.4 6.8 1.1 1. 0.54 E 0.46 U.38 • 0.014707+0.085915• x = 0.852573 0.30 3.2 3.6 4.0 4.4 4.8 5.2 5.6 6.0 6.4 6.8

=1/width

0.5

1.8 0.55555

3. 0.333333

5.6 2.

4.6 2.5 0.4

4.2

- 5 Press erri + 1 and select Add Data & Statistics. Construct a scatterplot of recipwidth (1/width) against length. The plot is now clearly linear.
- 6 Press menu>Analyze>Regression>Show Linear (a + bx) to plot the line on the scatterplot with its equation

Note: The y in the equation on the screen corresponds to the transformed variable 1/width

- 7 Write down the regression equation in terms of the variables width and length.
- 8 Substitute 5 cm for *length* in the equation.

 $1/width = 0.015 + 0.086 \times 5 = 0.445$ Thus width = 1/0.445 = 2.25 cm (to 2 d.p.)

 $1/width = 0.015 + 0.086 \times length$

3.6 Using the "BI Transformer Residual" template Steps

1. Enter new data into "xev", "yrv" columns (green boxes)

							- /	
∢ 1.	1	1.2	1.3	•Bl Mans	fual		RAD 📘 🕽	×
	A	xev	B yrv	BI Transf	D X.Y	E X	F x	
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1		1.	11.	Title	Linea	Linea	Linea	
2		2.	13.	RegE	a+b*	a+b*	a+b*	
3		З.	15.	a*y−	9.5	77.5	0.99	

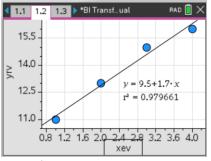
2. Transformed values will appear in columns E-J; r value and r^2 value can be found in rows 5 & 6 (blue and brown writing respectively); a & b can be found in rows 3 & 4 (pink writings) for equations.

∢ 1.	.1	1.2	1.3	*BI Tran:	sfual		RAD 📘	×
	A	xev	B yrv	С	D x.y	E x	F x	1
Ξ					=LinR	e=LinR	e=LinR	1
3		3.	15.	a*y−	9.5	77.5	0.99	
4		4.	16.	b*slo	1.7	46.1	0.05	
5		_	_	r²	0.97	0.98	0.96	
6			_	r	0.98	0.99	0.98	ľ

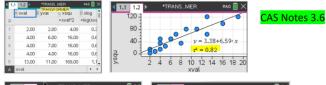
3. Bivariate data prediction Residual Actual Values can be found in Columns K L M (pink area)

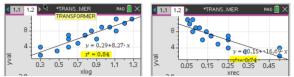
k	1.	.1 1.2	1.3 🕨	*Bl Tran	ısf ual	RAD [$ \times$
Γ					M actual		1
	=	=LinR(=d3+d	residual -	=residual+		
	1	_inea	11.2	-0.2	11.		
L	2	a+b*	12.9	0.1	13.		
	3	17 . 0	14.6	0.4	15.		
	4	-6 . 3	16.3	-0.3	16.		

4. Transformed data plot in page 1.2. Residual plot in page 1.3. Click on "xev" & "yrv" to choose right transformation to show corresponding equations and r^2 value.



5. Example Qs





 Apply the squared transformation to the variable ws3.00 pm and determine the equation of the least squares regression line that allows (ws3.00 pm)² to be predicted from ws9.00 am
 Wind speed (km/h)

 In the boxes provided, write the coefficients for this equation, correct to 3 significant figures.
 9.00 am
 3.00 pm

 2
 2

														4	6	
(ws3.00 pm) ² =	3.38	+	6.59		×	ws9	.00	am			r ² =0	.82		4	7	
														4	4	
(ws3.00 pm) =	0.29	+	8.27		× I	og(ws9	00	am)	r ² =	1 84	1	13	11	
(#35.00 pm) =	0.25		0.27		~ '	06(.00	un	<i>'</i>	,	5.04	\checkmark	6	7	
														3	3	
(ws3.00 pm) =	10.2	+	16.7		/ w	/s9.0	00 a	m			r ² =0).74		16	10	
				12	_	_	_	_	_	_		_		6	7	
											•		•	13	8	
				10	Γ							•		11	9	
				8	\vdash	+	-	•	-	-	•	+	-	2	4	
		win	id speed 3.00 pm (km/h)	6	L		1	t_						7	8	
			ws3.00pm				•							5	5	
				4	t	۰.	<u>†</u>			1		+		8	6	
				2	⊢	+	-	-	-	-	\vdash	+		6	7	
				0										19	11	
				0	ò	2	4 (2 14 m (km		18 20	9	9	
							wir			.00 a 20am						

3.7 Using "Slopey Predi" template

1. Two dots entering in green boxes and b slope and a y-intercept will come out in pink boxes

۹ i	1 🕨		SLOPEY	rad 📋 🗙			
	A	в	С	D	E	F	î
=							[
1	title	entry	title	resul	title	entry	
2	Xı	<u> </u>	b*slo		х	_	
3	Уı	_	a*y−i		у	_	
4	X2	_	b*slo	_	х	_	
5	y2	_	a*y−i	_	у	_	Ŧ

2. Following values entering green boxes, and b slope and a y-intercept will come out in above orange boxes

◀ 1.	1		SLOPEY	EDI		rad 📋 🗙		
Γ	A	в	С	D	E	F	1	
=								
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7	Sx	_						
8	Sy	_						
9	x	_						
10	ÿ	_					•	

3. Given values of \boldsymbol{x} or \boldsymbol{y} values entering to column F, prediction will come out inside pink boxes

€ 1.	.1 🕨		*SLOPEYE	DI	RAD 📘	×
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=						ľ
1	title	entry	prediction			
2	х	_	-			
3	у	_				
4	x	_				
5	у	_	_			

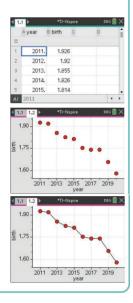
CAS 1: How to construct a time series using the TI-Nspire CAS

Construct a time series plot for the data presented below, which shows the birth rate in Australia (in births per woman) from 2011–2020.

year	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020
birth	1.926	1.920	1.855	1.826	1.814	1.752	1.741	1.740	1.657	1.580

Steps

- **1** Start a new document by pressing **etrl** + **N**.
- 2 Select Add Lists & Spreadsheet. Enter the data into lists named *year* and *birth*.
- Press ent + 1 and select Add Data & Statistics. Construct a scatterplot of *birth* against *year*. As is the case for a time series plot, *year* is the explanatory variable and *birth* the response variable.
- 4 To display as a connected time series plot, move the cursor to the main graph area and press etrl + memp>Connect Data Points. Press [enter].



4.2 Using the "Smoothie" template

Using the "smoothie" template

If all formulas are correct, the following results should be visible for the dataset provided. Check that your template has generated the same smoothed values. Then save the file again ([etr.] (S))

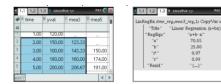
•	A time	^B yval	C mea3	D mea5	E med3	F med5	G mea4	H cmea4	1 med4	J cmed4
=										
1	1.00	120.00	142		122	-		1.541	1921	1.12
2	2.00	150.00	123.33		120.00		137.50		135.00	
3	3.00	100.00	143.33	150.00	150.00	150.00	157.50	147.50	165.00	150.00
4	4.00	180.00	160.00	174.00	180.00	180.00	180.00	168.75	190.00	177.50
5	5.00	200.00	206.67	191.00	200.00	200.00	213.75	196.88	217.50	203.75
6	6.00	240.00	225.00	220.00	235.00	235.00	230.00	221.88	237.50	227.50
7	7.00	235.00	240.00		240.00					
8	8.00	245.00								

The template can be used to:

find the correct smoothed values based on a given time period, or range of time periods

	hie 🔝 🛛 PAD 📢 💥			1.3 Esmooth		
mea3[4]	160.00	P	med3	F med5	G mea4	H cmea
cmed4[5]	203.75	=				
emed al al	2000/0	Э	150.00	150.00	157.50	147.
1		-4	180.00	180.00	180.00	168.
		5	200.00	200.00	213.75	196.
		6	235.00	235.00	230.00	221.
		7	240.00			
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	the effects and suit	ability	of var			
240 110 120 120 120 120 120 120 12		med4 Omed3	of var 240 - 210 - 180 - 150 -	tious smo		PAC

 create smoothed bivariate data sets upon which regression methods may be applied (would need to be copied and pasted to new lists to ensure that the two variables had same number of values, and lined up with time period correctly



VIP Notel: To use the template with a new time series, select the time column and press **A** until the entire column is selected. Then press menu > Data > Clear Data to clear the data (this does not delete the variable name, which is important as these names are used in the formulas in other columns). Repeat for the yval column, and then enter the data for the new time series.

RAD 🚺 🗙

147.50

168.75

196.88 4 >

J cmea4

137.50

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ove X Varia

οк Cance

"Linear Regression (a+bx)"

"a+b·x" -0.095317 0.01469

0.987778 0.99387

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DEG 🚺 🗙

9: Add Y Summary Lis A: Remove Y Variable

1: Plot Ty ~ 1: Connect Data

130.00

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3: Acti

4: Analy 5: Wind

6: Setting

36.8

36.5

Linear Regression (a+bx)

Save RegEqn to: Frequency List

Category List

1.4 1.5 1.6 ▶ Brake data
 □

LinRegBx spdsq, distance, 1: CopyVar stat. Re

Include Categories

"Title

"RegEqn" "a" "b"

"r²

"Resid'

X List: spdsq

Y List: distance

Using CAS SMOOTHIE to do 2/4-mean smoothing \bigcirc



4.3 Comparing two or three time series graphs

To get both temperature and threepointsmooth on the y-axis, follow these steps

To add a second y-variable, press:

- MENU menu .
- 2: Plot Properties 2
- . 6: Add Y Variable 6
- . Select threepointsmooth Enter enter

4.4 A full statistic display of LSRL

A full statistical display can be shown in a Calculator page using menu >Statistics>Stat Calculations>Linear Regression (a+bx).

Note: if you have performed a linear regression in the Data & Statistics page you can access the statistics in the Calculator page by pressing var >Stat Results.

The regression equation y=-0.0953+0.0147x in this case is:

distance= -0.0953 + 0.0147 speed squared

4.5 Using regression equation to predict

Use the regression equation to predict the stopping distance (to the nearest metre) of a car travelling at 50 km/h

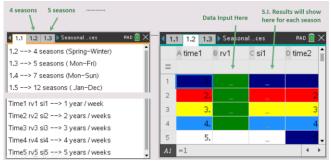
In the Calculator page recall the regression equation by pressing var and select stat.regeqn to paste to work area.

You need to add (x) after pasting as shown. When substituting in the speed value remember that the x now represents speed squared so enter as 50².

stat.RegEqn(x) x=50 ²	36.6301
0.01469 x-0.095317 x=50 ²	36.6297

Answer: 37 m (to the nearest metre)

4.6 Using "Seasoning" template



4.7 Using "Correct De Seasoning" template

Entering data into green area, answers come out in coloured area

4 1.	🖣 1.1 1.2 🕨 Correct Ding 😽 RAD 📘 🗙						×
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	(seasonal index - 1) × 100 =%						I
	A negative %: (season) is below the seasonal average \y% A positive %: (season) is above the seasonal average \y% Correcting for seasonality:						
	$\left(\frac{1}{seasonal\ index}-1\right) \times 100 = $ %						
	 A negative %: To correct (season) for seasonality, (unit) need to be decreased by % 						
- A	 A positive %: To correct (season) for seasonality, (unit) need to be increased by% 						
	Deseasonalised Figure = $\frac{Actual Figure}{S.I.}$ = Actual Figure + $\frac{1}{r_{s}}$						
Actu	Actual figure= Deseabonalised Figure * S.I.						

1a. Univariate Categorical Data: Frequency Table

The [types of categories] of [total frequency] [frequency type] were classified as [list of categories].

Modal Category

The majority of [frequency type], [modal percentage], were found to be [modal category].

Of the remaining [frequency types], [percentage X] were found to be [category X], while [percentage Y] were found to be [category Y], and while [etc.].

Equal Categories

The [frequency types] all had roughly the same percentages where [category X] had [percentage X], [category Y] had [percentage Y], [etc.].

1b. Univariate Numerical Data: Histogram, Dot Plot, Stem Plot

The shape of the distribution is [symmetric/positively skewed/negatively skewed] Refer to 1F: Describing numerical data

The distribution has a [standard dev./range/IQR] of [value]

The distribution has a [mean/median/mode] of [value]

The distribution [has #/has no] outliers.

1c. Univariate Numerical Data: Box Plot

The distribution is **[positively skewed/negatively skewed]** with **[outliers/no outliers]**. The distribution is centered at **[value]**, the median value. The spread of the distribution, is measured by the IQR, is **[value]** and, as measured by the range **[value]**. If outliers present: There are **[value]** many outliers: **[list of outliers]**

2a. Bivariate Data (Both Categorical): Two-way Frequency Table

Worked example: Is there an association between interest in sports and age group? Yes, the percentage of males with a high level of interest in sport steadily decreases with age group from 56.5 % for the 'under 18 years' age group, to 35.0% for the '36-50 years' age group.

	Age group (%)					
Interest in sport	Under 18 years		26–35 years			
High	56.5	50.2	40.7	35.0		
Medium	30.1	34.4	36.8	45.8		
Low	13.4	13.4	22.5	20.3		
Total	100.0	100.0	100.0	100.0		

2b. Bivariate Data (one categorical, One Numerical): Comparing two boxplots:

The distributions at [variable name] are [symmetric/positively skewed/negatively skewed] for both [boxplot variables]. There [are/are no] outliers. The median [variable name] is higher for [boxplot 1], (M= value), than [boxplot 2], (M= value). The IQR is also greater for [boxplot 1], (IQR= value), than [boxplot 2], (IQR= value). The range of [variable name] is also greater for [boxplot 1], (R= value), than [boxplot 2], (IQR= value). The range of [variable name] is also greater for [boxplot 1], (R= value), than [boxplot 2], (R= value).

2c. Bivariate Data (Both Numerical): Scatter Plot

There is a [strong/moderate/weak], [positive/negative],[linear/non-linear] relationship between [response variable y] and [explanatory variable x]. There [are/are no] clear outliers.

2d. The coefficient of determination (r²):

The coefficient of determination indicates that [r² x 100] % of the variation in [response variable] is explained by the variation in [explanatory variable] and [remaining %] is explained by other factors.

2e. Least squares line:

The equation of the regression line is: [response variable] = [a] + [b] x [explanatory variable]

Slope (b):

On average, [response variable] [increases/decreases] by [b units] for every one [unit] increase in [explanatory variable].

y- intercept (a):

When [explanatory variable] is 0, [response variable] is predicted to be [a units].

2f. Residual Plot

The residual plot shows a [random scatter/ curved pattern] indicating there is a [linear/non-linear] relationship between [response variable] and [explanatory variable].

2g. Prediction Reliability

The prediction using [explanatory variable] of [value of EV] is [reliable/ unreliable] as it is [within/ outside] the date range and is therefore [interpolation/extrapolation].

2h. The appropriateness of fitting a transformed regression analysis

Transformations are [appropriate/ not appropriate] as the original data produces a [non-linear/ linear] scatterplot, confirmed with a clear [curved pattern/ random scatter] in the residual plot.

[Log[EV]/Reciprocal [EV]/[EV]Squared/ Log[RV]/Reciprocal[RV]/[RV]Squared] is the most appropriate transformation, given it has the strongest coefficient of determination r^2 of $[r^2 \times 100]$ %, compared with $[r^2 \times 100]$ % and $[r^2 \times 100]$ %.

2i. A residual analysis on the number

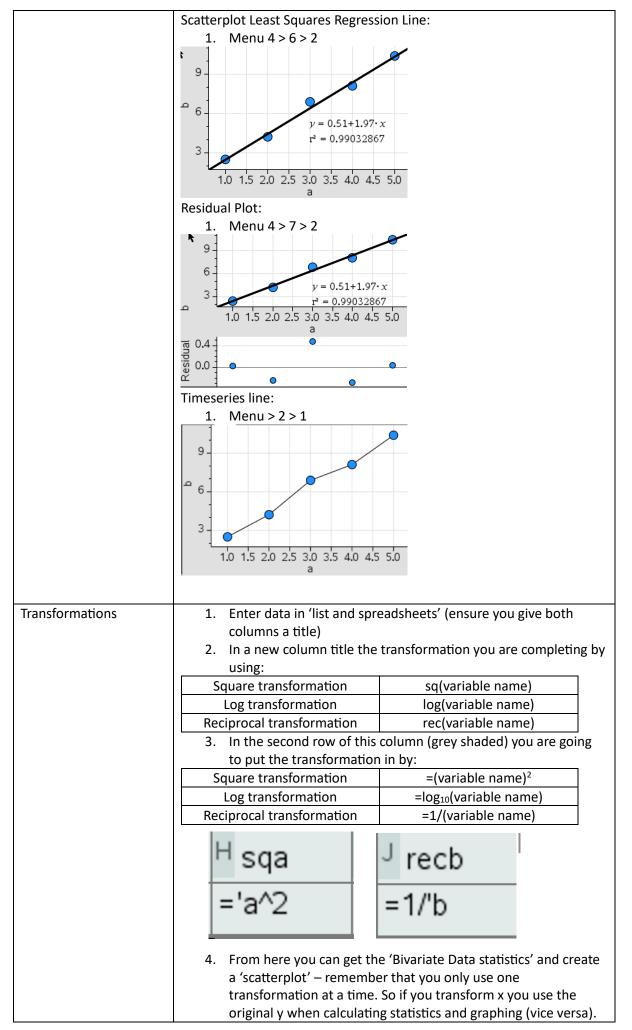
The residual value is [positive/ negative], [above/ below] the LSRL or the LSRL is an [under prediction/ over prediction].

2j. Confounding variables

Since the correlation coefficient [r value] indicates a [strong/moderate/weak] association. Therefore, factors (confounding variables) other than the [explanatory variable] must be considered. Some of these factors include [list potential reasons here].

CAS reference sheet: Data

Univariate Data	1. Ente	er data in 'list and spread	lsheets' (ensure	e you give it a t	itle)
Statistics: to find the 5	2. Menu > 4 > 1 > 1				
number summary, mean and standard	3. Select the title you gave the data in the 'X-List'				
deviation	MinX	1.	x		з.
	QıX	1.5	Σx		15.
	MedianX 3. Σx^2 5				
	Q ₃ X 4.5				
	MaxX 5. SX := Sn 1.58113 1. Enter data in 'list and spreadsheets' (ensure you give it a title)				
Graphing Univariate Data: dot plot, boxplots, histograms	 Ctrl 'dat. Click Mer Histogram so Mer Mer Wid 	doc or open a new page a and statistics' < to add data to the x-axi nu > 1 : choose the pot to	via the home r is ype you are afte r interval size. A axis	nenu and selec	ct
Graphing Bivariate Data: Grouped Bar Chart	Menu >	ate first Bar Chart 2 > 9 > select second set	OK Cancel		
Graphing Bivariate Data: parallel boxplots	 Create first boxplot Menu > 2 > 5 > select second set of data 				
Bivariate Data Statistics: a, b, r, r ²	 Enter data in 'list and spreadsheets' (ensure you give both columns a title) Menu > 4 > 1 > 4 (Spreadsheets); Menu > 6 > 1 > 4 (Calculator) Select your EV in the 'X-List' and your RV in the 'Y-List' 				
	Linear Regressio	.ist: 'a	RegEqn	a+b*x	
	1	.ist: b	а	0.51	
	Save RegEqn to: f1 b				,
	Category L	.ist:	r²	0.99032	
	Include Categor	ies: V	r	0.99515	
Scatterplots	colu 2. Ctrl 'dat	er data in 'list and spread Imns a title) doc or open a new page a and statistics' < to add the EV to the x-a	via the home r	nenu and seleo	



Solve	 Calculator Page Menu > 3 > 1 You write inside the brackets, there must be an equals sign (=), you must choose a variable (x) and then use the same variable
	at the end and do 'comma variable' (,x) solve $(10=x+2,x)$ x=8.
Mean Smoothing	 Enter values into list and spreadsheet in column A If 2 or 3 mean smoothing start in column B cell 2. If 4 or 5 mean smoothing start in column B cell 3 Write a. 2 mean = (a1+2a2+a3)/4 b. 3 mean = (a1+2a2+a3)/3 c. 4 mean = (a1+2a2+2a3+2a4+a5)/8 d. 5 mean = (a1+a2+a3+a4+a5)/5 Hover over the cell in the bottom right corner until the plus appears, click and drag and it will fill the values for you. Comparing time series plots: Menu > 2 > 6
Back to top of List	Ctrl 7